

may be traitors, trying to prevent the loyal generals from reaching agreement. The generals must have an algorithm to guarantee that

A. All loyal generals decide upon the same plan of action.

The loyal generals will all do what the algorithm says they should, but the traitors may do anything they wish. The algorithm must guarantee condition A regardless of what the traitors do.

The loyal generals should not only reach agreement, but should agree upon a reasonable plan. We therefore also want to insure that

B. A small number of traitors cannot cause the loyal generals to adopt a bad plan.

Condition B is hard to formalize, since it requires saying precisely what a bad plan is, and we do not attempt to do so. Instead, we consider how the generals reach a decision. Each general observes the enemy and communicates his observations to the others. Let $v(i)$ be the information communicated by the i th general. Each general uses some method for combining the values $v(1), \dots, v(n)$ into a single plan of action, where n is the number of generals. Condition A is achieved by having all generals use the same method for combining the information, and Condition B is achieved by using a robust method. For example, if the only decision to be made is whether to attack or retreat, then $v(i)$ can be General i 's opinion of which option is best, and the final decision can be based upon a majority vote among them. A small number of traitors can affect the decision only if the loyal generals were almost equally divided between the two possibilities, in which case neither decision could be called bad.

While this approach may not be the only way to satisfy conditions A and B, it is the only one we know of. It assumes a method by which the generals communicate their values $v(i)$ to one another. The obvious method is for the i th general to send $v(i)$ by messenger to each other general. However, this does not work, because satisfying condition A requires that every loyal general obtain the same values $v(1), \dots, v(n)$, and a traitorous general may send different values to different generals. For condition A to be satisfied, the following must be true:

1. Every loyal general must obtain the same information $v(1), \dots, v(n)$.

Condition 1 implies that a general cannot necessarily use a value of $v(i)$ obtained directly from the i th general, since a traitorous i th general may send different values to different generals. This means that unless we are careful, in meeting condition 1 we might introduce the possibility that the generals use a value of $v(i)$ different from the one sent by the i th general—even though the i th general is loyal. We must not allow this to happen if condition B is to be met. For example, we cannot permit a few traitors to cause the loyal generals to base their decision upon the values “retreat”, ..., “retreat” if every loyal general sent the value “attack”. We therefore have the following requirement for each i :

2. If the i th general is loyal, then the value that he sends must be used by every loyal general as the value of $v(i)$.